

$$x = x_0 + \int_{t_0}^t v_x dt \quad v_x = \frac{dx}{dt} \quad v_{x,avg} = \frac{\Delta x}{\Delta t} \quad \theta = \theta_0 + \int_{t_0}^t \omega dt \quad \omega = \frac{d\theta}{dt} \quad \omega_{avg} = \frac{\Delta\theta}{\Delta t}$$

$$v_x = v_{x0} + \int_{t_0}^t a_x dt \quad a_x = \frac{dv_x}{dt} \quad a_{x,avg} = \frac{\Delta v_x}{\Delta t} \quad \omega = \omega_0 + \int_{t_0}^t \alpha dt \quad \alpha = \frac{d\omega}{dt} \quad \alpha_{avg} = \frac{\Delta\omega}{\Delta t}$$

$$v_x = v_{x0} + a_x \Delta t$$

$$x = x_0 + v_{x0} \Delta t + \frac{1}{2} a_x (\Delta t)^2$$

$$v_x^2 = v_{x0}^2 + 2a_x \Delta x$$

Similar equations apply for motion along y and z.

$$\omega = \omega_0 + \alpha \Delta t$$

$$\theta = \theta_0 + \omega_0 \Delta t + \frac{1}{2} \alpha (\Delta t)^2$$

$$\omega^2 = \omega_0^2 + 2\alpha \Delta\theta$$

$$a_{rad} = v^2 / R = \omega^2 R$$

$$a_{tan} = \alpha R$$

$$v_{tan} = \omega R$$

$$s = \theta R$$

$$\vec{F}_{net} = m\vec{a}$$

$$\vec{\tau}_{net} = I\vec{\alpha}$$

$$w = mg \text{ OR } F_g = Gm_1 m_2 / r^2 \quad \vec{F}_{spring} = -k(\Delta\vec{x})$$

$$\vec{\tau} = \vec{r} \times \vec{F}$$

$$f_s \leq \mu_s n \quad f_k = \mu_k n \quad f_r = \mu_r n$$

$$\text{where } |\vec{\tau}| = I\alpha = rF \sin\phi = rF_{tan}$$

$$f_{drag} = kv \text{ (low speed) OR } f_{drag} = Dv^2 \text{ (high speed)}$$

$$I = \sum_i m_i r_i^2$$

$$\Delta K = W_{total}$$

$$W_c = -\Delta U$$

$$W_{NC} = -\Delta U_{int} = \Delta E \text{ where } E = K + U$$

$$\Delta K + \Delta U + \Delta U_{int} = 0$$

$$K_i + U_i + W_{NC} = K_f + U_f$$

$$K_{trans} = \frac{1}{2} mv^2$$

$$K_{rot} = \frac{1}{2} I\omega^2$$

$$W = \int_{s_i}^{s_f} \vec{F} \cdot d\vec{s} \quad P = \frac{dW}{dt} = \vec{F} \cdot \vec{v}$$

$$W = \int_{\theta_i}^{\theta_f} \tau_z d\theta \quad P = \frac{dW}{dt} = \tau_z \omega_z$$

$$U_g = mgy \text{ OR } U_g = -Gm_1 m_2 / r \quad U_{elastic} = \frac{1}{2} k(\Delta x)^2$$

$$F_x(x) = \frac{-dU(x)}{dx}$$

$$\vec{p} = m\vec{v}$$

$$\vec{L} = \vec{r} \times \vec{p} = \vec{r} \times m\vec{v} = I\vec{\omega}$$

$$\vec{F}_{net} = \frac{d\vec{p}}{dt} \quad \vec{J} = \int_{t_i}^{t_f} \vec{F}_{net} dt = \Delta\vec{p}$$

$$\vec{\tau}_{net} = \frac{d\vec{L}}{dt}$$

$I\omega$  applies only for a rigid body around an axis of symmetry

$$p = p_0 + \rho gh$$

$$F_B = m_{fl,disp} g = \rho_{fl} V_{fl,disp} g$$

$$\frac{dV}{dt} = Av = \text{constant}$$

$$p + \rho gy + \frac{1}{2} \rho v^2 = \text{constant}$$

Simple harmonic oscillator:  $x(t) = A \cos(\omega t + \phi_0)$

$$\omega = 2\pi f = 2\pi / T \quad \text{where } \omega = \sqrt{k/m} \text{ (spring-mass)}$$

$$\text{OR } \omega = \sqrt{k/I} \text{ (torsion spring)}$$

$$\text{OR } \omega = \sqrt{g/L} \text{ (simple pendulum)}$$

$$\text{OR } \omega = \sqrt{mgd/I} \text{ (physical pendulum)}$$

Slightly damped oscillator:  $x(t) = Ae^{-(0.5b/m)t} \cos(\omega' t + \phi_0)$

$$\text{where } \omega' = \sqrt{\frac{k}{m} - \frac{b^2}{4m^2}}$$

$$y(x,t) = A \cos\left[2\pi\left(\frac{x \mp vt}{\lambda}\right)\right] = A \cos\left[2\pi\left(\frac{x}{\lambda} \mp \frac{t}{T}\right)\right] = A \cos(kx \mp \omega t) \quad \text{where } k = 2\pi / \lambda \quad \text{and} \quad v = \lambda / T = \lambda f$$

transverse, string/spring:  $v = \sqrt{T/\mu}$

$$P_{avg} = \frac{1}{2} \omega^2 A^2 \sqrt{\mu T}$$

longitudinal, fluid or bulk solid:  $v = \sqrt{B/\rho}$

$$I = \frac{1}{2} \omega^2 A^2 \sqrt{\rho B} = p_{max}^2 / (2\rho v) \quad \text{where } p_{max} = 2\pi BA / \lambda$$

$$I_1 / I_2 = r_2^2 / r_1^2$$

$$\beta = (10 \text{ dB}) \log(I / I_0)$$

$$y(x,t) = A_{sw} \sin(kx + \phi_0) \sin(\omega t) \quad \text{where } A_{sw} = 2A \text{ (standing wave)}$$

$$f_n = n \frac{v}{2L} = n f_1 \quad \lambda_n = 2L / n \quad \text{where } n = 1, 2, 3, \dots \text{ (string or open pipe)}$$

$$f_n = n \frac{v}{4L} = n f_1 \quad \lambda_n = 4L / n \quad \text{where } n = 1, 3, 5, \dots \text{ (stopped pipe)}$$

$$\Delta L = \alpha L_0 \Delta T \quad \Delta V = \beta V_0 \Delta T \quad Q = mc\Delta T \quad \text{OR} \quad Q_{V \text{ or } p} = nC_{V \text{ or } p} \Delta T \quad \text{OR} \quad Q = \pm mL$$

$$H = \frac{dQ}{dt} = kA(T_H - T_C)/L \text{ (conduction)} \quad \text{OR} \quad H = \frac{dQ}{dt} = Ae\sigma T^4 \quad \text{AND} \quad H_{NET} = Ae\sigma(T^4 - T_s^4) \text{ (radiation)}$$

$$pV = nRT = Nk_B T \quad \left\langle \frac{1}{2}mv^2 \right\rangle_{\text{avg}} = \frac{1}{2}mv_{\text{rms}}^2 = \frac{3}{2}k_B T \quad K_{\text{total}} = \frac{3}{2}Nk_B T = \frac{3}{2}nRT$$

$$\lambda = \frac{V}{(4\pi\sqrt{2})^2 N} \quad u_{\text{int}} \text{ (per degree of freedom per molecule)} = \frac{1}{2}k_B T \quad C_V = (\# \text{ degrees of freedom})R/2$$

$$\Delta U = Q - W \quad \Delta U = nC_V \Delta T \quad W = \int_{V_1}^{V_2} p dV$$

$$pV^\gamma = \text{constant}, \text{ where } \gamma = C_p / C_V \text{ (adiabatic)} \quad C_p = C_V + R \text{ (ideal gas)}$$

$$e = \frac{W}{Q_H} = 1 - \left| \frac{Q_C}{Q_H} \right| \quad e_{\text{Carnot}} = 1 - \frac{T_C}{T_H} \quad K = \frac{|Q_C|}{|W|} = \frac{|Q_C|}{|Q_H| - |Q_C|} \quad W = nRT \ln \left( \frac{V_2}{V_1} \right) \left\{ \begin{array}{l} \text{isothermal} \\ \text{process} \end{array} \right.$$

### Useful Constants & Conversions

$$g = 9.8 \text{ m/s}^2$$

$$G = 6.673 \times 10^{-11} \text{ N m}^2 / \text{kg}^2$$

$$I_0 = 1.0 \times 10^{-12} \text{ W / m}^2$$

$$\sigma = 5.67 \times 10^{-8} \text{ W / m}^2 \cdot \text{K}^4$$

$$R = 8.31 \text{ J / mol} \cdot \text{K}$$

$$k_B = 1.38 \times 10^{-23} \text{ J / K}$$

$$N_A = 6.02 \times 10^{23} \text{ molecules/mol}$$

$$p_{\text{atm}} = 1.013 \times 10^5 \text{ Pa} = 1 \text{ atm}$$

$$T(\text{K}) = T(^{\circ}\text{C}) + 273.15 \text{ K}$$

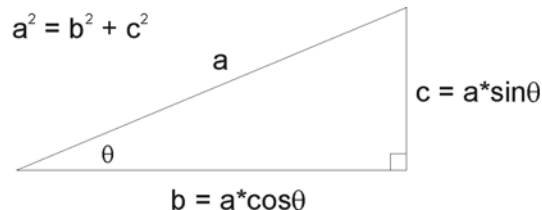
$$1 \text{ L} = 10^{-3} \text{ m}^3$$

### Moments of Inertia

slender rod (length $L$ ), through center	$I = \frac{1}{12}ML^2$
slender rod (length $L$ ), through end	$I = \frac{1}{3}ML^2$
rectangular plate ( $a$ by $b$ ), through center	$I = \frac{1}{12}M(a^2 + b^2)$
rectangular plate ( $a$ by $b$ ), along edge $b$	$I = \frac{1}{3}Ma^2$
hollow cylinder (inner radius $R_1$ , outer $R_2$ )	$I = \frac{1}{2}M(R_1^2 + R_2^2)$
solid cylinder, (radius $R$ )	$I = \frac{1}{2}MR^2$
thin-walled hollow cylinder, (radius $R$ )	$I = MR^2$
solid sphere (radius $R$ )	$I = \frac{2}{5}MR^2$
thin-walled hollow sphere (radius $R$ )	$I = \frac{2}{3}MR^2$

### Algebra and trigonometry

$$ax^2 + bx + c = 0 \Rightarrow x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$



### Astronomical Data

	Mass (kg)	Radius (m)	Orbit radius (m)	Orbit period
Sun	$1.99 \times 10^{30}$	$6.96 \times 10^8$	-----	-----
Moon	$7.35 \times 10^{22}$	$1.74 \times 10^6$	$3.84 \times 10^8$	27.3 days
Mercury	$3.30 \times 10^{23}$	$2.44 \times 10^6$	$5.79 \times 10^{10}$	88.0 days
Venus	$4.87 \times 10^{24}$	$6.05 \times 10^6$	$1.08 \times 10^{11}$	224.7 days
Earth	$5.97 \times 10^{24}$	$6.38 \times 10^6$	$1.50 \times 10^{11}$	365.3 days
Mars	$6.42 \times 10^{23}$	$3.40 \times 10^6$	$2.28 \times 10^{11}$	687.0 days
Jupiter	$1.90 \times 10^{27}$	$6.91 \times 10^7$	$7.78 \times 10^{11}$	11.86 yrs
Saturn	$5.68 \times 10^{26}$	$6.03 \times 10^7$	$1.43 \times 10^{12}$	29.45 yrs
Uranus	$8.68 \times 10^{25}$	$2.56 \times 10^7$	$2.87 \times 10^{12}$	84.02 yrs
Neptune	$1.02 \times 10^{26}$	$2.48 \times 10^7$	$4.50 \times 10^{12}$	164.8 yrs
Pluto	$1.31 \times 10^{22}$	$1.15 \times 10^6$	$5.91 \times 10^{12}$	247.9 yrs

\*\*\* For each body, "radius" is its radius at the equator and "orbit radius" is its average distance from the sun (for the planets) or from the earth (for the moon).